

# PIB '20 P5 - 4D Matrices

**Time limit:** 0.5s    **Memory limit:** 256M

You are given a grid  $d$  of size  $N \times (N - 1)$ .

Using this grid, you are to generate a new grid  $a$  of size  $N \times N$  as follows:

1. The first element in each row  $i$  will be assigned a value of  $v_i$ . The array  $v$  is unknown to you.
2. For each element  $2 \leq j \leq N$  in row  $i$ ,  $a_{i,j} = a_{i,j-1} + d_{i,j-1}$ .

A third array,  $k$  will then be generated as follows:

1. The  $i^{\text{th}}$  element is the *median* of the  $i^{\text{th}}$  column in  $a$ .

It is known that the *median* of the array  $k$  is **exactly** zero. Can you determine any array  $v$  that makes the median of  $k$  zero, or state that it is impossible?

**Note:** For odd  $N$ , the median of the array is the middle element in the sorted array. For even  $N$ , the median is the *minimum* of the two middle elements in the sorted array. For example, the median of  $[1, 6, 4, 3]$  is 3.

## Input Specification

The first line will contain the integer  $N$  ( $2 \leq N \leq 1000$ ).

The next  $N$  lines will each contain  $N - 1$  integers,  $d_{i,j}$  ( $|d_{i,j}| \leq 10^5$ ).

## Output Specification

If it is impossible, print  on one line.

Otherwise, print  on the first line.

On the second line, print  $N$  space separated integers, the array  $v$ .  $v_i$  must fit in a 32-bit integer ( $-2^{31} \leq v_i < 2^{31}$ ), or you will receive .

## Subtasks

### Subtask 1 [7%]

$N \leq 5, d_{i,j} \geq 0$

### Subtask 2 [24%]

$d_{i,j} \geq 0$

### Subtask 3 [69%]

No additional constraints.

## Sample Input for Subtask 1

---

```
4
2 1 0
3 3 0
1 6 1
1 1 1
```

## Sample Output for Subtask 1

---

```
YES
-1 -3 -2 0
```

## Explanation for Sample for Subtask 1

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The array  $a$  that is generated with the array  $k$  below is:

```
-1  1  2  2
-3  0  3  3
-2 -1  5  6
 0  1  2  3
-----
-2  0  2  3
```

The median of the array  $k$  is 0. Note that there could be multiple answers. For example,  $[-2, -3, -3, 0]$  is also an answer. You are only required to print *any* one of them.

## Sample Input for Subtask 2

---

```
7
1 2 2 2 1 1
3 0 0 1 1 1
0 0 0 0 0 0
1 0 2 1 0 1
2 0 0 1 4 0
2 1 1 2 4 5
1 1 1 1 1 1
```

## Sample Output for Subtask 2

---

```
YES
5 1 -2 -3 1 -5 -8
```

## Sample Input for Subtask 3

---

```
3
3 -12
-6 3
6 -5
```

## Sample Output for Subtask 3

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```
YES
-1 5 -1
```