

# NOI '22 P1 - Major

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**Time limit:** 1.5s    **Memory limit:** 1G

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In this problem, the mode of a sequence is the number that appears strictly more than half the times in the sequence. Please refer to this definition in the problem.

Initially,  $n$  positive integer sequences of different lengths are given, numbered from 1 to  $n$ , and the sequences can be empty. These  $n$  sequences are considered to exist, and the sequences corresponding to other numbers are considered to be non-existent.

There are  $q$  operations, and operations are of the following types:

- 1  $x y$ : Insert the number  $y$  at the end of sequence  $x$ . It is guaranteed that sequence  $x$  exists and  $1 \leq x, y \leq n + q$ .
- 2  $x$ : Delete the number at the end of sequence  $x$ . It is guaranteed that sequence  $x$  exists, is not empty, and  $1 \leq x \leq n + q$ .
- 3  $m x_1 x_2 \dots x_m$ : Concatenate sequences  $x_1, x_2, \dots, x_m$  to get a new sequence and return its mode. Return -1 if the mode does not exist. The data guarantees that for any  $1 \leq i \leq m$  the sequence numbered  $x_i$  still exists,  $1 \leq x_i \leq n + q$ , and the concatenated sequence is non-empty. There is no guarantee that  $x_i$  are distinct. The concatenation done here won't affect future operations.
- 4  $x_1 x_2 x_3$ : Create a new sequence numbered  $x_3$ , which is the concatenation of sequence  $x_1$  and sequence  $x_2$ . Then, delete the sequences numbered  $x_1$  and  $x_2$ . After this operation, sequence  $x_3$  is considered to exist, and the sequences  $x_1$  and  $x_2$  are considered to be non-existent and will not be used again in subsequent operations. It is guaranteed that  $1 \leq x_1, x_2, x_3 \leq n + q$ ,  $x_1 \neq x_2$ , the sequences  $x_1$  and  $x_2$  existed before the operation, and no operation used the sequence numbered  $x_3$  before the operation.

## Input Specification

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The first line of input contains two positive integers  $n$  and  $q$ , which represent the number of initial sequences and the number of operations, respectively. It is guaranteed that  $n, q \leq 5 \times 10^5$ .

In the next  $n$  lines, the  $i$ -th line represents the sequence numbered  $i$ . The first non-negative integer  $l_i$  of each line represents the length of the  $i$ -th sequence, followed by  $l_i$  non-negative integers  $a_{i,j}$  representing the elements of the sequence in order. Let  $C_i = \sum l_i$  represent the sum of the input sequence lengths, then it is guaranteed that  $C_i \leq 5 \times 10^5$  and  $a_{i,j} \leq n + q$ .

Each of the next  $q$  lines represent an operation in the format described above, consisting of several integers. Let  $C_m = \sum m$  represent the sum of all sequences that need to be concatenated in operation 3, then it is guaranteed that  $C_m \leq 5 \times 10^5$ .

## Output Specification

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For each type 3 query, output an integer on a new line, the answer to the query.

## Samples

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Sample inputs and outputs can be found [here](#).

## Sample Input 1

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```
2 8
3 1 1 2
3 3 3 3
3 1 1
3 1 2
4 2 1 3
3 1 3
2 3
3 1 3
1 3 1
3 1 3
```

## Sample Output 1

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```
1
3
-1
3
-1
```

## Explanation for Sample 1

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The first query queries the mode of sequence 1. Since the sequence contains two 1s, more than half the length of the sequence, the mode is 1. The second query queries the mode of sequence 2. Since the sequence contains only 3s, the mode is 3. The third query asks for the mode of sequence 3. At this time, sequence 3 is (1, 1, 2, 3, 3, 3), and there is no number occurring more than 3 times, so the output is `-1`.

## Sample Input 2

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```
4 9
1 1
1 2
1 3
1 4
3 4 1 2 3 4
1 1 2
3 2 1 2
2 3
3 3 1 2 3
1 4 4
1 4 4
1 4 4
3 4 1 2 3 4
```

## Sample Output 2

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```
-1
2
2
4
```

## Explanation of Sample 2

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The first query asks for the mode obtained after concatenating sequences 1, 2, 3, 4. The result of concatenation is (1, 2, 3, 4), and there is no number with more than two occurrences, so the output is `-1`. The fourth query is the mode of the sequence obtained after concatenating sequences 1, 2, 3, 4. The result of the concatenation is (1, 2, 2, 4, 4, 4, 4), which has a mode of 4.

## Sample 3

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See `major3.in` and `major3.ans` in the attachment package. This example satisfies the constraints of test cases 1~3.

## Sample 4

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See `major4.in` and `major4.ans` in the attachment package. This example satisfies the constraints of test cases 11~12.

## Constraints

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For all test data, it is guaranteed that  $1 \leq n, q, C_m, C_l \leq 5 \times 10^5$ .

Test Case	$n, q, C_m, C_l \leq$	Additional Constraints
1~3	300	Property C
4~7	4000	Property C
8	$10^5$	Property A, B
9		Property A
10		Property B
11, 12		Property C
13		None
14		$5 \times 10^5$
15	Property A	
16	Property B	
17, 18	Property C	
19, 20	None	

Special properties:

- Property A:  $n = 1$ , no operations of type 4.
- Property B: At any time, the sequences contain only 1s and 2s.
- Property C: No operations of type 2.