

# Longest Balanced Subsequence

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**Time limit:** 0.15s    **Memory limit:** 64M

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You are given a one-indexed string of brackets of length  $N$ . A string of brackets is considered "balanced" if it is classified in one of the three categories listed below:

1. It is an empty string.
2. It has the form of  $(A)$ , where  $A$  is a balanced string.
3. It has the form  $AB$ , where  $A$  and  $B$  are both balanced strings.

For example,  $(()())$  is balanced, but  $()()()$  is not. A subsequence of a string is a string obtained by deleting some (possibly zero) characters of the string. Please note that a subsequence does **not** have to be contiguous. You are to write a program that supports  $Q$  of the following two operations:

1. Output the length of the longest balanced subsequence of the substring from index  $L_i$  to  $R_i$  inclusive.
2. Flip the bracket located at index  $P_i$ . (i.e. from  $()$  to  $()$  and vice versa)

## Constraints

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$$1 \leq N, Q \leq 10^5$$

$$1 \leq L_i \leq R_i \leq N$$

$$1 \leq P_i \leq N$$

### Subtask 1 [30%]

$$1 \leq N, Q \leq 10^3$$

### Subtask 2 [70%]

No additional constraints.

## Input Specification

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The first line of input will contain two integers  $N$  and  $Q$ , the length of the string and the number of operations.

The second line will contain a string of length  $N$ , the initial sequence of brackets. The string will only contain  $()$  and  $()$ .

Each of the next  $Q$  lines will start with either 1 or 2. If it starts with 1, two integers  $L_i$  and  $R_i$  will follow. If it starts with 2, one integer  $P_i$  will follow.

## Output Specification

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For each type 1 operation, print one line containing the length of the longest balanced subsequence.

## Sample Input

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```
10 7
()))((()((
1 5 8
1 3 6
1 1 10
2 10
1 9 10
2 3
1 1 10
```

## Sample Output

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```
4
0
6
2
10
```

## Explanation

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For the first type 1 query, the whole substring `((()))` is balanced.

For the second type 1 query, there exists no balanced subsequence with positive length.

For the third type 1 query, the required subsequence `()((()))` goes from index 1 to 2, then 5 to 8.

For the fourth type 1 query, the whole substring `()` is balanced after the update.

For the fifth type 1 query, the whole string `((()((()((()((` is balanced after the second update.