

# DMOPC '18 Contest 1 P4 - Sorting

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**Time limit:** 1.0s    **Memory limit:** 256M

Java: 2.5s

Python: 2.5s

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You have a sorted list  $A$  of numbers in increasing order from 1 to  $N$ . This list has  $M$  elements. Some numbers may appear multiple times, so you have recorded the number of occurrences of each number in this list,  $f_1, f_2, \dots, f_N$ . However, you messed up when assigning the indices, so  $f_i$  is actually the number of occurrences of  $P_i$ , for some unknown permutation  $P$  of  $1, 2, \dots, N$ . You recall that  $A_K = X$  for some  $K$  and  $X$ . Find a permutation  $P$  that satisfies this. If no such permutation  $P$  exists, output  $-1$ .

**You will be rewarded even if you can only determine the existence of such a  $P$ .** Outputting any permutation of  $1, 2, \dots, N$  if there exists a permutation and  $-1$  otherwise for every test case of a subtask will earn you half of the subtask's points, assuming you do not already receive the full points (if one of the permutations outputted is wrong, but there does exist a permutation).

## Constraints

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$$1 \leq X \leq N$$

$$1 \leq K \leq M \leq 2 \cdot 10^{11}$$

$$1 \leq f_i \leq 1\,000\,000$$

$$f_1 + f_2 + \dots + f_N = M$$

### Subtask 1 [10%]

$$1 \leq N \leq 8$$

### Subtask 2 [20%]

$$1 \leq N \leq 20$$

### Subtask 3 [20%]

$$1 \leq N \leq 400$$

### Subtask 4 [10%]

$$1 \leq N \leq 2\,000$$

### Subtask 5 [40%]

$$1 \leq N \leq 200\,000$$

## Input Specification

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The first line will contain four space-separated integers  $N$ ,  $M$ ,  $K$ , and  $X$ .

The next line will contain  $N$  space-separated integers  $f_1, f_2, \dots, f_N$ .

## Output Specification

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If there exists a permutation, output  $N$  space-separated integers  $P_1, P_2, \dots, P_N$ . There may be many valid permutations. Any one of them will be accepted.

If there does not exist a permutation, output `-1`.

## Sample Input 1

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```
3 10 5 1
4 5 1
```

## Sample Output 1

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```
2 1 3
```

## Explanation for Sample 1

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There are six possible lists  $A$ :

```
1 1 1 1 2 2 2 2 2 3
1 1 1 1 2 3 3 3 3 3
1 1 1 1 1 2 2 2 2 3
1 1 1 1 1 2 3 3 3 3
1 2 2 2 2 3 3 3 3 3
1 2 2 2 2 2 3 3 3 3
```

The third list satisfies  $A_K = X$ . The corresponding  $P$  which gives this list is  $2, 1, 3$ .

## Sample Input 2

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```
6 9 4 4
2 2 2 1 1 1
```

## Sample Output 2

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```
4 5 6 1 2 3
```

### Sample Input 3

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```
6 9 3 4  
2 2 2 1 1 1
```

### Sample Output 3

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```
-1
```