CEOI '22 P4 - Drawing

Time limit: 1.5s   **Memory limit:** 512M

Paint & Wine is the first painting studio in Zagreb offering relaxing painting lessons with a glass of wine on the side. During the lesson, students are given a certain theme, and with the aid of master painters usually manage to paint an impressive piece.

Ante is a master painter, Luka is his student, and this task tells the tale of a lesson that included a bit more wine than usual.

Ante: "Paint me a tree!"

Luka: "Alright. What kind of tree do you want? Palm, oak, pine. . . ?"

Ante: "I want a connected acyclic undirected graph!"

Luka: "I can do that. . . Any other wishes?"

Ante: "I like it when no node is adjacent to more than three other nodes!"

Luka: "Uhm, okay. . .Well, there are many such trees."

Ante: "Here is a list of edges, I want that one!"

Luka: "Ok, wow. Still, there are many ways to draw it."

Ante: "Here is a list of points in the plane where I want the nodes to be drawn. I also don't want to see a pair of intersecting edges."

Luka: "I'm on it!"

Your task is to help Luka paint the tree according to Ante's wishes. More precisely, given a description of a tree, such that no node is adjacent to more than three other nodes, and a list of points in the plane, find a one-to-one mapping of nodes to points such that, when edges of the tree are drawn as line segments between corresponding points, they do not intersect (except at end points).

Input Specification

The first line of input contains an integer N, the number of nodes in the tree and the number of points in the plane.

The following $N - 1$ lines describe edges of the tree, one per line. Each edge is described by two integers a and b, labels of nodes connected by the edge. Nodes are labelled with integers from 1 to N.

It is guaranteed that each node is adjacent to at most three other nodes.

The following N lines contain the points to be used when drawing the tree, one per line. Each point is described by a pair of integer coordinates. No two points share the same pair of coordinates, and **no three points lie on the same line**.

Output Specification

Output a permutation of integers from 1 to N in a single line. The i-th number should be the label of the node which is mapped to the i-th input point.

If there are multiple valid solutions, output any of them. It's guaranteed that a solution always exists.

Constraints

For all subtasks:

Point coordinates are integers between 0 and 10^9.

Subtask	Score	Constraints
1	10	$3 \le N \le 200\,000$, there exists a convex polygon with the given points as vertices
2	15	$1 \le N \le 4\,000$
3	15	$1 \le N \le 10\,000$
4	35	$1 \le N \le 80\,000$
5	25	$1 \le N \le 200\,000$

Sample Input 1

```
3
1 2
2 3
10 10
10 20
20 10
```

Sample Output 1

```
1 2 3
```

Sample Input 2

```
5
1 2
1 3
1 4
4 5
10 10
10 30
30 10
30 30
20 25
```

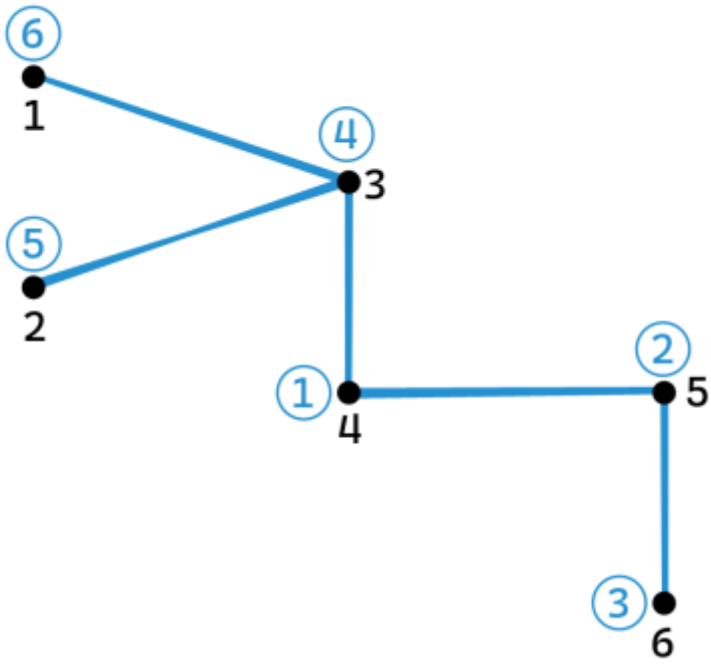## Sample Output 2

```
5 4 2 3 1
```

Sample Input 3

```
6
1 2
2 3
1 4
4 5
4 6
10 60
10 40
40 50
40 30
70 30
70 10
```

Sample Output 3

```
6 5 4 1 2 3
```

Explanation for Sample 3

Blue numbers represent node labels while black numbers represent point indices.